



Answer the following questions

Illustrate your answers with sketches when necessary

[1] Question One: (15 Marks)

- a) A two-port network is driven at both ports such that the port voltages and currents have the following values ($Z_0 = 50 \Omega$):

$$\begin{aligned} V_1 &= 10 \angle 90^\circ & ; & & I_1 &= 0.2 \angle 90^\circ \\ V_2 &= 8 \angle 0^\circ & ; & & I_2 &= 0.16 \angle -90^\circ \end{aligned}$$

Determine the input impedance seen at each port, and find the incident and reflected voltages at each port. **(5 Marks)**

- b) The input and output matching networks in a silicon BJT microwave amplifier are designed to produce $\Gamma_s = 0.5 \angle 120^\circ$ and $\Gamma_L = 0.4 \angle 90^\circ$. (i) Determine the power gain, the available power gain, the transducer power gain if the scattering parameters of the transistor are: $S_{11} = 0.6 \angle -160^\circ$, $S_{12} = 0.045 \angle 16^\circ$, $S_{21} = 2.5 \angle 30^\circ$, and $S_{22} = 0.5 \angle -90^\circ$. (ii) Calculate the power available from the source, P_{avs} , the average power delivered to the network, P_m , the power available from the network, P_{avn} , and the power delivered to the load, P_L , if $V_s = 10 \angle 0^\circ$, $Z_s = 50 \Omega$, and $Z_L = 50 \Omega$. **(10 Marks)**

[2] Question Two: (15 Marks)

- a) Use the μ -parameter test to determine which of the following devices are unconditionally stable and, of those, which has the greatest stability: **(5 Marks)**

Device	S_{11}	S_{12}	S_{21}	S_{22}
A	$0.34 \angle -170^\circ$	$0.06 \angle 70^\circ$	$4.3 \angle 80^\circ$	$0.45 \angle -25^\circ$
B	$0.75 \angle -60^\circ$	$0.2 \angle 70^\circ$	$5.0 \angle 90^\circ$	$0.51 \angle 60^\circ$
C	$0.65 \angle -140^\circ$	$0.04 \angle 60^\circ$	$2.4 \angle 50^\circ$	$0.70 \angle -65^\circ$

- b) Using the scattering parameter data for the GaAs MESFET given in the following table, design an amplifier for maximum gain at 8.0 GHz. Design matching sections using open-circuited shunt stubs, and compute the gain. **(10 Marks)**

f (GHz)	S_{11}	S_{12}	S_{21}	S_{22}
4.0	$0.72 \angle -103^\circ$	$0.12 \angle 28^\circ$	$2.91 \angle 86^\circ$	$0.53 \angle -68^\circ$
8.0	$0.52 \angle 179^\circ$	$0.14 \angle -1^\circ$	$2.0 \angle 20^\circ$	$0.42 \angle -129^\circ$
12.0	$0.49 \angle 103^\circ$	$0.17 \angle -19^\circ$	$1.5 \angle -38^\circ$	$0.44 \angle 170^\circ$

[3] Question Three: (20 Marks)

- a) Design a bandpass filter having a 0.5 dB equal-ripple response, with $N = 3$. The center frequency is 1 GHz, the bandwidth is 10%, and the impedance is 50Ω . **(10 Marks)**
- b) Design an amplifier to have a gain of 10 dB at 6.0 GHz, using a transistor with the following scattering parameters ($Z_0 = 50 \Omega$): **(10 Marks)**

S_{11}	S_{12}	S_{21}	S_{22}
$0.61 \angle -170^\circ$	0	$2.24 \angle 32^\circ$	$0.72 \angle -83^\circ$

Plot (and use) constant-gain circles for $G_S = 1$ dB and $G_L = 2$ dB. Use matching sections with open-circuited shunt stubs.

[4] Question Four: (20 Marks)

- a) Design a high-pass lumped-element filter with a 3 dB equal-ripple response, a cutoff frequency of 3 GHz, and at least 30 dB insertion loss at 2.0 GHz. The characteristic impedance is 75Ω . **(10 Marks)**
- b) A GaAs FET has the following scattering parameters and noise parameters at 6.0 GHz ($Z_0 = 50 \Omega$): **(10 Marks)**

S_{11}	S_{12}	S_{21}	S_{22}
$0.6 \angle -60^\circ$	0	$2.0 \angle 81^\circ$	$0.7 \angle -60^\circ$

$F_{\min} = 2.0$ dB, $\Gamma_{\text{opt}} = 0.62 \angle 100^\circ$, and $R_N = 20 \Omega$. Design an amplifier to have a gain of 6 dB and the minimum noise figure possible with this gain. Use open-circuited shunt stubs in the matching sections.

Hints:

$$G = \frac{P_L}{P_{\text{in}}} = \frac{|S_{21}|^2 (1 - |\Gamma_L|^2)}{(1 - |\Gamma_{\text{in}}|^2) |1 - S_{22}\Gamma_L|^2}$$

$$G_A = \frac{P_{\text{avn}}}{P_{\text{avs}}} = \frac{|S_{21}|^2 (1 - |\Gamma_S|^2)}{|1 - S_{11}\Gamma_S|^2 (1 - |\Gamma_{\text{out}}|^2)}$$

$$G_T = \frac{P_L}{P_{\text{avs}}} = \frac{|S_{21}|^2 (1 - |\Gamma_S|^2) (1 - |\Gamma_L|^2)}{|1 - \Gamma_S\Gamma_{\text{in}}|^2 |1 - S_{22}\Gamma_L|^2}$$

$$\left| \Gamma_L = \frac{(S_{22} - \Delta S_{11}^*)^*}{|S_{22}|^2 - |\Delta|^2} \right| = \left| \frac{S_{12}S_{21}}{|S_{22}|^2 - |\Delta|^2} \right|$$

$$(\Gamma_{\text{in}} - \Delta S_{11}^*)\Gamma_S^2 + (|\Delta|^2 - |S_{11}|^2 + |S_{22}|^2 - 1)\Gamma_S + (S_{11}^* - \Delta^* S_{22}) = 0$$

$$g_S = \frac{G_S}{G_{S_{\max}}} = \frac{1 - |\Gamma_S|^2}{|1 - S_{11}\Gamma_S|^2} (1 - |S_{11}|^2)$$

$$g_L = \frac{G_L}{G_{L_{\max}}} = \frac{1 - |\Gamma_L|^2}{|1 - S_{22}\Gamma_L|^2} (1 - |S_{22}|^2)$$

$$\left| \Gamma_S = \frac{g_S S_{11}^*}{1 - (1 - g_S)|S_{11}|^2} \right| = \frac{\sqrt{1 - g_S} (1 - |S_{11}|^2)}{1 - (1 - g_S)|S_{11}|^2}$$

$$N = \frac{|\Gamma_S - \Gamma_{\text{opt}}|^2}{1 - |\Gamma_S|^2} = \frac{F - F_{\min}}{4R_N/Z_0} |1 + \Gamma_{\text{opt}}|^2$$

$$\left| \Gamma_S = \frac{\Gamma_{\text{opt}}}{N + 1} \right| = \frac{\sqrt{N(N + 1 - |\Gamma_{\text{opt}}|^2)}}{(N + 1)}$$